# **Mathsarc Education**

A learning place to fulfill your dream of success!

### **HOMEWORK SHEET**

#### **NUMBER SYSTEM**



## SINGLE OPTION CORRECT

1.	$\frac{\left(2^{n+4}-2(2^n)\right)}{2(2^{n+3})} - \frac{1}{2(2^{n+3})}$	+ 2 <sup>-3</sup>	is equal t	0
----	---	-------------------	------------	---

- (A)  $2^{n+1}$
- (B)  $-2^{n+1} + \frac{1}{8}$  (C)  $\frac{9}{8} 2^n$
- (D) 1

The least number, which divided by 48, 60, 72, 108 and 140 leaves 38, 50, 62, 98 and 130 respectively, is

- (A) 11115
- (B) 15110
- (C) 15120
- (D) 15210

3. Which of the following statement is true?

(A) Every point on the number line represents a rational number.

(B) Irrational number cannot be represented by points on the number line

(C)  $\frac{22}{7}$  is a rational number

(D) None of these

4. If  $2 = x + \frac{1}{1 + \frac{1}{3 + \frac{1}{4}}}$ , then value of x is

- $(A)^{\frac{12}{17}}$
- (B)  $\frac{13}{17}$

 $(C)^{\frac{18}{17}}$ 

(D)  $\frac{21}{17}$ 

The LCM of two numbers is 14 times of their HCF. The sum of LCM and HCF is 600. If one of the number is 80, then other number is

- (A) 280
- (B) 218

(C) 25

(D) 45

6. If the HCF of 468 and 222 expressed as 468x + 222y where x, and y are integers then the value of

(y-x) is

(A) 27

(B) 35

(C) 30

(D) 28

7. Find the unit digit of the expression  $(272)^{353} + (23)^{258} + (137)^{137} + (158)^{248}$  is:

(A) 1

(B)2

(C) 3

(D) 4

 $\chi^{\left(\frac{a+b-c}{(a-c)(b-c)}\right)}.\chi^{\left(\frac{b+c-a}{(b-a)(c-a)}\right)}.\chi^{\left(\frac{c+a-b}{(c-b)(a-b)}\right)}$  is equal to

- (A)  $x^{a+b+c}$
- (B) x

(C) 1

(D) 0

9. If 
$$\left(\frac{x^{-1}y^2}{x^2y^{-4}}\right)^7 \div \left(\frac{x^3y^{-5}}{x^{-2}y^3}\right)^{-5} = x^p \cdot y^q$$
 then the value of p and q are

- (A) p = 1, q = 1 (B) p = 2, q = 1
- (C) p = 4, q = 1
- (D) p = 2, q = 2

- 10. If  $x = a + \sqrt{a^2 + 1}$  then a in terms of x
  - $(A)^{\frac{x^2-1}{2x}}$
- (B)  $\frac{x^2+1}{2x}$

- (C)  $\frac{x^2-1}{2}$
- (D)  $\frac{x^2-3}{2}$

- 11. If  $x = 5 + 2\sqrt{6}$ , then  $\sqrt{\frac{x}{2}} \frac{1}{\sqrt{2x}} =$ 
  - (A)360
- (B) 720

(C) 540

(D) 1440

12. If 
$$\sqrt{\frac{6+2\sqrt{3}}{33-19\sqrt{3}}} = a + b\sqrt{3}$$
, then  $a + b =$ 

(A)6

(B) 8

(C) 10

(D) 12

13. 
$$\frac{1}{1+x^{a-b}} + \frac{1}{1+x^{b-a}}$$
 is equal to

- $(A)\frac{x^{ab}}{x^{a}+x^{b}}$

(C) 1

(D)  $\frac{x^{ab}}{x^{b-a}}$ 

14. 
$$\sqrt{6 + \sqrt{6 + \sqrt{6 + \sqrt{6 + \dots \dots \dots \infty}}}}$$
 is equal to

(A)3

(B) 2

(C) 1

 $(D) \pm 3$ 

15. When simplified, the product 
$$\left(1-\frac{1}{3}\right)\left(1-\frac{1}{4}\right)\left(1-\frac{1}{5}\right)\left(1-\frac{1}{6}\right).....\left(1-\frac{1}{n}\right)$$
 equals to

 $(A)^{\frac{1}{n}}$ 

- $(C)^{\frac{2(n-1)}{n}}$
- (D)  $\frac{2}{n(n+1)}$
- 16. Which option is true for  $\sqrt{2x^2 1 + 2x\sqrt{x^2 1}} = \cdots \dots \dots$ 
  - (A)  $x \sqrt{x^2 1}$  (B)  $x + \sqrt{x^2 1}$  (C)  $x + \sqrt{x^2 + 1}$  (D)  $x \sqrt{x^2 + 1}$

17. If 
$$\left[ \frac{\left\{ 1 - \left( \frac{a}{b} \right)^{-2} \right\} a^2}{\left( \sqrt{a} - \sqrt{b} \right)^2 + 2\sqrt{ab}} \right] = 1$$
 and  $a + b = 5$  where  $a, b \in \mathbb{R}^+$ , then value of  $a^b - b^a$  is

(A)1

(B) 2

(C) 0

- (D) -1
- 18. The value of  $\frac{1}{\sqrt{3}+\sqrt{2}-1}$  on simplifying upto 3 decimal places, given that  $\sqrt{2}=1.4142$  and  $\sqrt{6}=2.4495$  is
  - (A) 0.166
- (B) 0.366
- (C) 0.466
- (D) 0.566
- 19. If R "Every fraction is a rational number", and T "Every rational number is a fraction", then which of the following is correct?
  - (A) R is true and T is false

(B) R is false and T is true

(C) Both R and T is true

(D) Both R and T is false

20.	ii m and n are i	if m and n are natural numbers such that $2^m - 2^n = 960$ then $(m + n)$ is equal to									
	(A) 10		(B) 15			(C) 16		(D) 20			
21.	If $1 \le k \le 25$ , he	ow many	prime	e numbers are tl	here v	which are o	of the form 6k	+ 1	?		
	(A) 15		(B) 16			(C) 17		(D) 18			
22.	22. If a, b, c and d are four positive real numbers such that sum of a, b and c is even and the sum d is odd, then $a^2 - d^2$ is necessarily										
	(A) Odd		(B) Even			(C) Prime		(D) Either A or B			
23.	In a class there are 72 boys and 64 girls. If the class is to be divided into least number of groups such that each group contains either only boys or only girls, then how many groups will be formed?										
	(A) 17		(B) 3	4		(C) 24			(D) None		
24.	If HCF of 858 and 325 can be expressed in the form $858m + 325n$ where $m, n \in \mathbb{Z}$ .										
	Find the value of $m + n$ .										
	(A) 10		(B) 20			(C) 30		(D) 40			
25.	Find $(x + y)$ if $x + \sqrt{3} + 2)y + (5 + \sqrt{3})(2x + 1)$ where $x, y \in Q$										
	(A) 1		(B) 0			(C) -1			(D) 2		
26.	In a $\triangle ABC$ , $\angle A =$	= <i>x</i> °,∠ <i>B</i> =	y° an	$d \angle C = (y + 20)$	)°. If 4	4x - y = 10	0, then the tria	angle	e is		
	(A) Right angle	d	(B) (	Obtuse angled		(C) Equila	teral Angled		(D) None of the	hese	
27.	How can the rel	ationship	betwo	een $x$ and $y$ be l	best d	lefined, if v	values of $x$ and	d y a	are as follows	as	
	x	2		3	4		5	6			
	у	0		2	6		12	2	0.0		
	(A) y = 2x - 4		(B) y	$= x^2 - 3x + 2$		$(C) y = x^2$	$x^2 - 4x$	(D)	$y = x^2 - 4$		
28.	The solution $(x, y, z)$ of the equations: $\frac{x}{4} = \frac{y}{3} = \frac{z}{2}$ , $7x + 8y + 5z = 62$ is										
	(A) (2,3,4)		(B) (3	3,4,2)		(C) (4,2,3)		(D)	(4,3,2)		
29.	9. Find the value of $(x - y)$ if $\frac{1}{2(2x+3y)} + \frac{12}{7(3x-2y)} = \frac{1}{2}$ and $\frac{7}{(2x+3y)} + \frac{4}{(3x-2y)} = 2$										
	(A) - 1		(B) 0			(C) 1		(D) None of these			
30.	Find the number factors of 1080										
	(A) 32		(B) 28			(C) 24		(D) 36			

#### **INTEGER TYPE**

- 1. If  $x = 8 \sqrt{60}$  and  $\frac{1}{2} \left[ \sqrt{x} + \frac{2}{\sqrt{x}} \right] = \sqrt{a}$  then find the value of 'a'
- 2. If  $a = \frac{1}{3-2\sqrt{2}}$  and  $b = \frac{1}{3+2\sqrt{2}}$  then  $a^2b + ab^2$  is equal to \_\_\_\_\_
- 3. Find the total number factor of 540.
- 4. The least multiple of 7, which leaves a remainder of 4, when divided by 6, 9, 15 and 18 is
- 5.  $\frac{3\sqrt{2}}{\sqrt{6}-\sqrt{3}} \frac{4\sqrt{3}}{\sqrt{6}-\sqrt{2}} + \frac{2\sqrt{3}}{\sqrt{6}+\sqrt{2}}$  is equal to
- 6. Find the sum of factors of 270.
- 7. If  $a = \frac{1}{3 2\sqrt{2}}$ ,  $b = \frac{1}{3 + 2\sqrt{2}}$  then the value of  $a^3 + b^3$  is
- 8. If the number 2345p60q is exactly divisible by 3 and 5, then the maximum value of p + q is
- 9. If  $1 \le k \le 25$ , how many prime numbers are there which are of the form (6k + 1)?
- 10. Mr. Elon wanted to type of first 180 natural number. Find the number of times he had to press the numbered keys.
- 11. If  $\left\{ (2^4)^{\frac{1}{2}} \right\}^x = 256$  then the value of *x* is



ining piace to fiufiii youn areams of suc



Keep smiling!

Visit Us: https://www.mathsarc.com

### ANSWER KEY & SOLUTION

#### SINGLE OPTION CORRECT

1. D 5. A 9. C 13. C

17. A 21. B 25. C 29. C

2. B 6. D 10. A

14. A 18. C 22. A 26. A

30. B

3. C 7. D 11. B

15. B 19. A 23. A

12. B 16. B 20. C 24. D 27. B 28. D

#### **INTEGER TYPE**

1. 5 5. 0 9. 16 2. 6 6.

10. 432

3. 24 7. 24

11. 4

4. 364

4. D

8. C

8. 13